

# INTRODUCTION TO SCILAB

## APPLICATION TO FEEDBACK CONTROL

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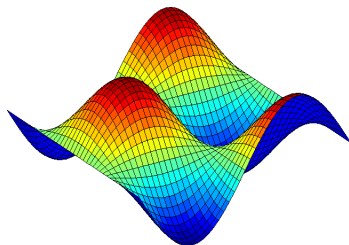
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## What is Scilab ?

Scilab is the contraction of *Scientific Laboratory*. Scilab is :

- a numerical computing software,
- an interpreted programming environment,
- used for any scientific and engineering applications,
- multi-platform : Windows, MacOS et Linux,

Created by researchers from Inria in the 90's, the software is now developed by Scilab Entreprises



[www.scilab.org](http://www.scilab.org)

Scilab includes hundreds of functions for various applications

- Mathematics and simulation
- 2D and 3D visualization
- Optimization
- Statistics
- Control system design and analysis
- Signal processing
- Application development

More informations : [www.scilab.org](http://www.scilab.org)

# License



- Scilab is an *open source* software.
- It is distributed under a GPL-compatible license.
- It is a free open source alternative to MATLAB<sup>®</sup> <sup>1</sup>.
- Scilab can be downloaded from :

`http://www.scilab.org/download/`

The version used in this introduction is

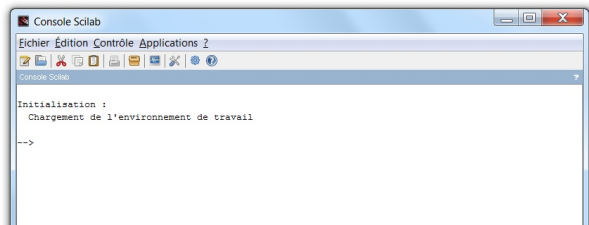
`version 5.4.1`

---

1. MATLAB is a registered trademark of The MathWorks, Inc.

## Getting started

Firstly, Scilab can be used in an interactive way by typing instructions on the console.



- type scilab code on the prompt -->
- type **enter**, to execute it.
- Scilab return its answer on the console or in a new window for graphics.

A first simple example :

```
--> A = 2;  
--> t = [0:0.01:10];  
--> y = A*sin(3*t);  
--> plot(t,y);
```

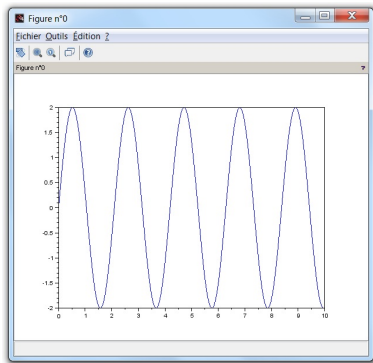
- Line 1 : assign the value 2 to the variable  $A$ .
- Line 2 : define a vector  $t$  that goes from 0 to 10 with a step of 0.01.
- Line 3 : compute a vector  $y$  from some mathematical operations.
- Line 4 : plot  $y$  with respect to  $t$  on a 2D graphic.

Note that “;” prevents from printing the result of an instruction.



A first simple example :

```
--> A = 2;  
--> t = [0:0.01:10];  
--> y = A*sin(3*t);  
--> plot(t,y);
```



A second simple example :

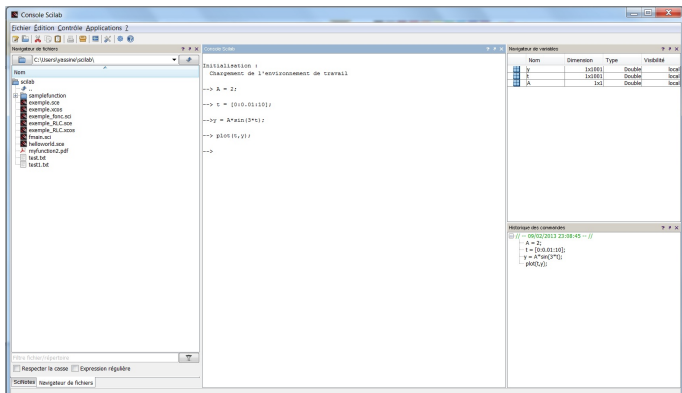
Let consider a system of linear equations

$$\begin{cases} 2x_1 + x_2 & = & -5 \\ 4x_1 - 3x_2 + 2x_3 & = & 0 \\ x_1 + 2x_2 - x_3 & = & 1 \end{cases}$$

Let solve it with Scilab

```
--> A = [2 1 0 ; 4 -3 2 ; 1 2 -1];  
--> b = [-5;0;1];  
--> x = inv(A)*b  
x  
=  
  1.75  
 - 8.5  
 - 16.25
```

Scilab provides a graphical environment with several windows.



- the console
- command history
- file browser
- variable browser
- and others : editor, graphics, help, ...

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# Elementary operations

Simple numerical calculations :

```
--> (1+3)*0.1
ans =
    0.4

--> 4^2/2
ans =
    8.

--> 2*(1+2*i)
ans =
    2. + 4.i

--> %i^2
ans =
    - 1.

--> cos(3)^2 + sin(3)^2
ans =
    1.

--> exp(5)
ans =
    148.41316

--> abs(1+i)
ans =
    1.4142136
```

## elementary operations

+	addition
-	subtraction
*	multiplication
/	right division
\	left division
^	exponents

## elementary functions

sin	cos	tan	cotg
asin	acos	atan	sec
sinh	cosh	tanh	csc
abs	real	imag	conj
exp	log	log10	log2
sign	modulo	sqrt	lcm
round	floor	ceil	gcd

```
--> conj(3+2*i)
ans =
    3. - 2.i

--> log10(10^4)
ans =
    4.
```

## boolean operations

- the boolean value *true* is written : %T.
- the boolean value *false* is written : %F.

&	logical <i>and</i>
	logical <i>or</i>
~	logical <i>not</i>
==	equal
~= or <>	different
< (<=)	lower than (or equal)
> (>=)	greater than (or equal)

```
--> %T & %F
ans =
F

--> 2 == 2
ans =
T

--> 2 < 3
ans =
T
```

## Variables

A variable can be directly defined via the assignment operator : “ = ”

```
--> a = 2.5;  
--> b = 3;  
--> c = a*b  
c  
    7.5  
  
--> c+d  
    !--error 4  
Undefined variable : d
```

- Variable names may be defined with letters  $a \rightarrow z$ ,  $A \rightarrow Z$ , numbers  $0 \rightarrow 9$  and few additional characters  $\%$ ,  $\_$ ,  $!$ ,  $\#$ ,  $?$ ,  $\$$ .
- Scilab is case sensitive.
- Do not confused the assignment operator “ = ” with the mathematical equal.
- Variable declaration is implicit, whatever the type.



## Pre-defined variables

<code>%i</code>	imaginary number $i = \sqrt{-1}$
<code>%e</code>	Euler's number $e$
<code>%pi</code>	constant $\pi$
<code>%inf</code>	infinity $\infty$
<code>%t</code> ou <code>%T</code>	boolean true
<code>%f</code> ou <code>%F</code>	boolean false

```
--> cos(2*%pi)
ans =
    1.

--> %i^2
ans =
   - 1.
```

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## Defining and handling vectors

A vector is defined by a list of numbers between brackets :

```
--> u = [0 1 2 3]
u
0.    1.    2.    3.
```

Automatic creation

```
--> v = [0:0.2:1]
v
0.    0.2    0.4    0.6    0.8    1.
```

Syntax : `start:step:end`

Mathematical functions are applied element-wise

```
--> cos(v)
ans
1.    0.980    0.921    0.825    0.696    0.540
```

column vectors can also be defined with semi colon separator “ ; ”

```
--> u = [1;2;3]
u
  1.
  2.
  3.
```

Some useful functions :

<b>length</b>	return the length of the vector
<b>max</b>	return the maximal component
<b>min</b>	return the minimal component
<b>mean</b>	return the mean value
<b>sum</b>	return the sum of all components
<b>prod</b>	return the product of all components

```
--> length(v)
ans =
  6.

--> mean(v)
ans =
  0.5
```

## Defining and handling matrices

Matrices are defined row by row with the separator “;”

```
--> A = [1 2 3 ; 4 5 6 ; 7 8 9]
A
  1.    2.    3.
  4.    5.    6.
  7.    8.    9.
```

Particular matrices :

<code>zeros(n,m)</code>	$n \times m$ matrix of zeros
<code>ones(n,m)</code>	$n \times m$ matrix of ones
<code>eye(n,n)</code>	identity matrix
<code>rand(n,m)</code>	$n \times m$ matrix of random numbers (values $\in [0, 1]$ )

Accessing the elements of a matrix :  $\mathbf{A}(\textit{select row}(s), \textit{select column}(s))$

```
--> A(2,3)
ans =
    6.

--> A(2,:)
ans =
    4.    5.    6.

--> A(:, [1 3])
ans =
    1.    3.
    4.    6.
    7.    9.
```

For vectors, one argument is enough  $\mathbf{v}(3)$  (gives 0.4)

Elements may be modified

```
--> A(2,3) = 0;
--> A
A =
    1.    2.    3.
    4.    5.    0.
    7.    8.    9.
```

Some useful functions :

<b>size</b>	return the dimensions of a matrix
<b>det</b>	compute the determinant of a matrix
<b>inv</b>	compute the inverse matrix
<b>rank</b>	return the rank of a matrix
<b>diag</b>	extract the diagonal of a matrix
<b>triu</b>	extract the upper triangular part of a matrix
<b>tril</b>	extract the lower triangular part of a matrix
<b>spec</b>	return the eigenvalues of a matrix

```
--> B = [1 0 ; 2 2];
--> det(B)
ans =
    2.

--> inv(B)
ans =
    1.    0.
   -1.    0.5

--> triu(A)
ans =
    1.    2.    3.
    0.    5.    6.
    0.    0.    9.
```

## Matrix operations

Basic operations  $+$ ,  $-$ ,  $*$ ,  $/$ ,  $^$  can be directly performed

- Watch out for dimension compatibility!
- transpose operator : “.’” , transpose and conjugate operator : “.’”

```
--> C = [ 1 0 ; 3 1 ; 0 2];
--> D = [1 1 ; 4 0];
--> B + D
ans =
    2.    1.
    6.    2.

--> B * inv(B)
ans =
    1.    0.
    0.    1.

--> A * C
ans =
    7.    8.
   19.   17.
   31.   26.

--> A + B
      !--error 8
Inconsistent addition.
```



Elementary functions are applied element-wise

```
--> M = [0 %pi/2 ; -%pi/2 %pi ];
--> sin(M)
ans =
    0.    1.
   -1.    1.225D-16

--> t = [0:0.2:1];
--> exp(t)
ans =
    1.    1.2214    1.4918    1.8221    2.2255    2.7182
```

There are specific versions of those functions for matrix operations

expm	logm	sqrtn
sinm	cosm	^

## Element-wise operations

<code>.*</code> <code>./</code> <code>^</code>
--

```
--> A = [0 4 ; 1 2];
--> B = [1 2 ; 5 -3];
--> A * B
ans =
    20.   -12.
    11.    -4.

--> A .* B
ans =
    0.    8.
    5.   -6.

--> A.^2
ans =
    0.   16.
    1.    4.

--> exp(t)./(t+1)
ans =
    1.    1.0178    1.0655    1.1388    1.2364    1.3591
```

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## 2D graphics

To plot a curve in the x-y plan use function `plot`

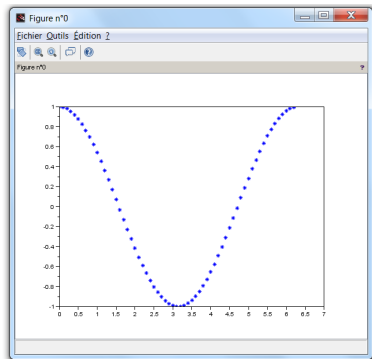
```
--> x = [0:0.1:2*%pi];  
--> y = cos(x);  
--> plot(x,y,'*')
```

## 2D graphics

To plot a curve in the x-y plan use function `plot`

```
--> x = [0:0.1:2*%pi];  
--> y = cos(x);  
--> plot(x,y,'*')
```

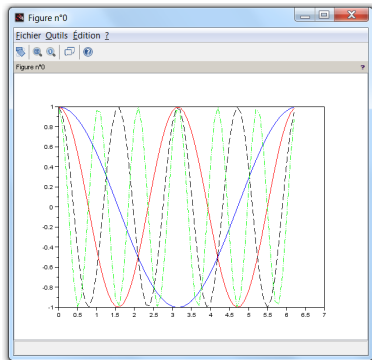
- `plot` traces a point for each couple  $x(i)$ - $y(i)$ .
- $x$  and  $y$  must have the same size.
- By default, a line is drawn between points.
- The third argument defines the style of the plot.



```
--> x = [0:0.1:2*%pi];  
--> y2 = cos(2*x);  
--> y3 = cos(4*x);  
--> y4 = cos(6*x);  
--> plot(x,y1);  
--> plot(x,y2,'r');  
--> plot(x,y3,'k:');  
--> plot(x,y4,'g--');
```

```
--> x = [0:0.1:2*%pi];  
--> y2 = cos(2*x);  
--> y3 = cos(4*x);  
--> y4 = cos(6*x);  
--> plot(x,y1);  
--> plot(x,y2,'r');  
--> plot(x,y3,'k:');  
--> plot(x,y4,'g--');
```

- Several graphics can be displayed.
- `clf` : clear the current graphic figure.



## 3D graphics

To plot a parametric curve in 3D space use function : `param3d`

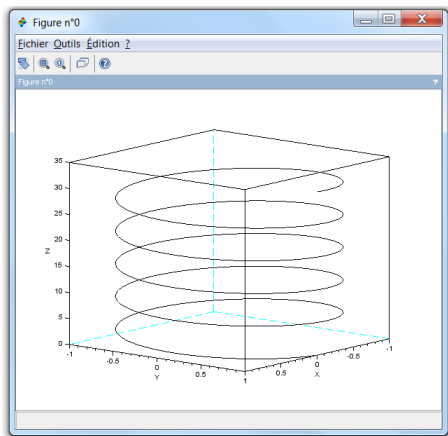
```
--> t = 0:0.01:10*%pi;  
--> x = sin(t);  
--> y = cos(t);  
--> z = t;  
--> param3d(x,y,z);
```



## 3D graphics

To plot a parametric curve in 3D space use function : `param3d`

```
--> t = 0:0.01:10*%pi;  
--> x = sin(t);  
--> y = cos(t);  
--> z = t;  
--> param3d(x,y,z);
```

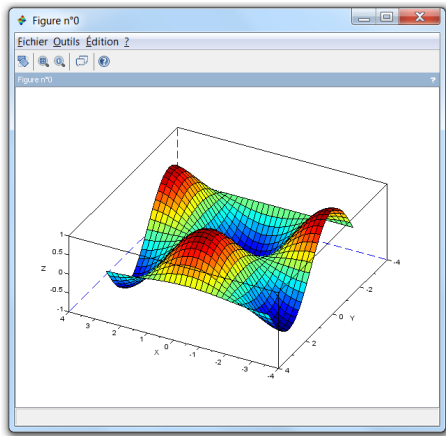


To plot a surface in 3D space use function : **surf**

```
--> x = [-%pi:0.2:%pi];  
--> y = [-%pi:0.2:%pi];  
--> [X,Y] = meshgrid(x,y);  
--> Z = cos(X).*sin(Y);  
--> surf(X,Y,Z)  
--> f=gcf();  
--> f.color_map = jetcolormap(32);
```

To plot a surface in 3D space use function : **surf**

```
--> x = [-%pi:0.2:%pi];  
--> y = [-%pi:0.2:%pi];  
--> [X,Y] = meshgrid(x,y);  
--> Z = cos(X).*sin(Y);  
--> surf(X,Y,Z)  
--> f=gcf();  
--> f.color_map = jetcolormap(32);
```



## Overview

Scilab provides several graphical functions :

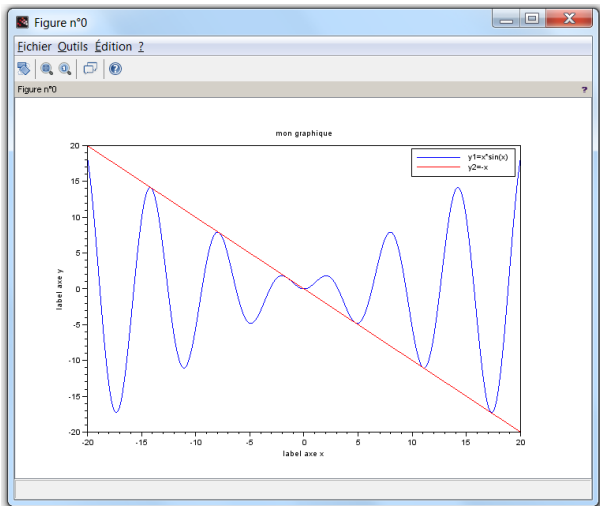
<code>plot</code>	2D graphic
<code>contour</code>	level curves in x-y plan
<code>surf</code>	3D surface
<code>pie</code>	“pie” plot
<code>histplot</code>	histogram plot
<code>hist3d</code>	3D histogram plot
<code>bar</code>	bar plot
<code>polarplot</code>	polar coordinate plot

Some instructions allow to add features to the figure :

<code>title</code>	add a title
<code>xtitle</code>	add a title and labels on axis
<code>legend</code>	add a legend

```
--> x = linspace(-20,20,1000);  
--> y1 = x.*sin(x);  
--> y2 = -x;  
--> plot(x,y1,'b',x,y2,'r')  
--> xtitle('mon graphique', 'label_␣axe_␣x', 'label_␣axe_␣y');  
--> legend('y1=x*sin(x)', 'y2=-x');
```

```
--> x = linspace(-20,20,1000);  
--> y1 = x.*sin(x);  
--> y2 = -x;  
--> plot(x,y1,'b',x,y2,'r')  
--> xtitle('mon graphique', 'label_axe_x', 'label_axe_y');  
--> legend('y1=x*sin(x)', 'y2=-x');
```



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## Scripts

A script is a set of instructions gathered in a file.

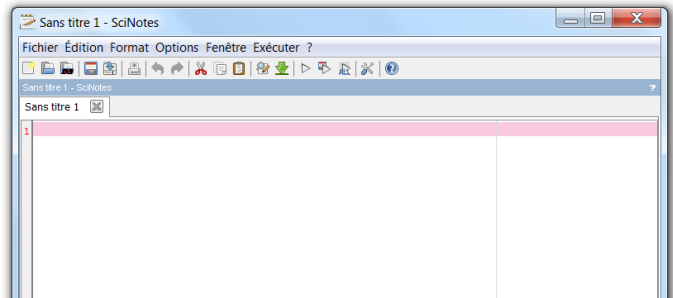
- Scilab provides a programming language (interpreted).
- Scilab includes an editor, but any text editor may be used.
- File extension should be “.sce” (but this is not mandatory).
- Editor launched from “*Applications > SciNotes*” or by typing `editor` on the console.



# Scripts

A script is a set of instructions gathered in a file.

- Scilab provides a programming language (interpreted).
- Scilab includes an editor, but any text editor may be used.
- File extension should be “.sce” (but this is not mandatory).
- Editor launched from “*Applications > SciNotes*” or by typing `editor` on the console.



## Example of a script : `myscript.sce`

```
// radius of a sphere
r = 2;

// calculation of the area
A = 4*pi*r^2;

// calculation of the volume
V = 4*pi*r^3/3;

disp(A, 'Area:');

disp(V, 'Volume:');
```

On the console :

```
-->exec('myscript.sce', -1)

Area:

    50.265482

Volume:

    33.510322
```

The file must be located in the *current directory*

- Comments : words following `//` are not interpreted.
- The current directory can be modified in menu *File* of the console.
- The path may be specified instead

```
exec('C:\Users\yassine\scilab\myscript.sce', -1)
```

- Scripts may also be run from the shortcut in the toolbar.
- Variables defined in the workspace (from the console) are visible and can be modified in the script.

Another example : `myscript2.sce`

```
x1 = -1; x2 = 1;
x = linspace(x1,x2,n);

y = exp(-2*x).*sin(3*x);

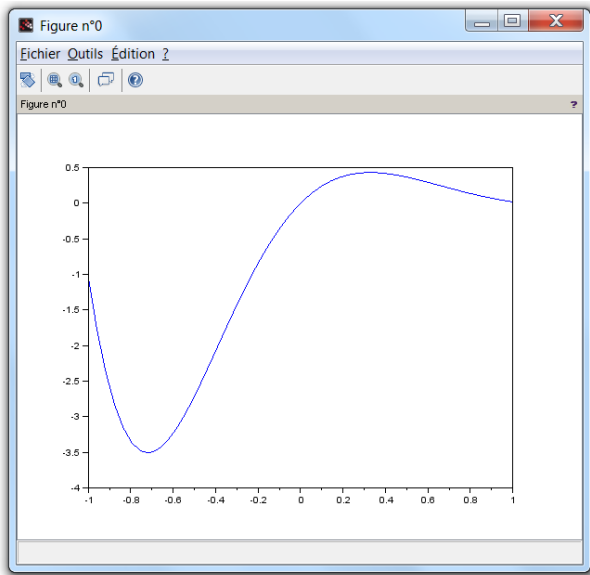
plot(x,y);
disp('see plot on the figure');
```

On the console :

```
--> n = 50;
-->exec('myscript2.sce', -1)

see plot on the figure
```

Here the variable `n` must be defined beforehand.



## Looping and branching

Scilab language includes classical control structures

Conditional statements **if**

```
if  boolean expression  then
    instructions 1
else
    instructions 2
end
```

```
if (x>=0) then
    disp("x is positive");
else
    disp("x is negative");
end
```

## Branching with respect to the value of a variable `select`

```
select  variable
case  value 1
    instructions 1
case  value 2
    instructions 2
else
    instructions 3
end
```

```
select i
case 1
    disp("One");
case 2
    disp("Two");
case 3
    disp("Three");
else
    disp("Other");
end
```

Loop control statements **for**

```
for   variable = start: step: end  
  
      instructions  
  
end
```

```
n = 10;  
for k = 1:n  
    y(k) = exp(k);  
end
```



Loop control based on a boolean expression **while**

```
while   (boolean expression)  
  
        instructions  
  
end
```

```
x = 16;  
while ( x > 1 )  
    x = x/2;  
end
```

And also :

- instruction **break** interrupt and exit a loop.
- instruction **continue** skip to the next iteration of a loop.

Note that as much as possible, use vector / matrix operations instead of loops. The code may run 10 to 100 times faster. This feature of Scilab is known as the *vectorization*.

```
tic
S = 0;
for k = 1:1000
    S = S + k;
end
t = toc(); disp(t);

tic
N = [1:1000];
S = sum(N);
t = toc(); disp(t);
```

```
-->exec('myscript.sce', -1)
```

```
0.029
```

```
0.002
```

## Functions

A function is a command that makes computations from variables and returns a result

```
outvar = afunction(invar)
```

- `afunction` is the name of the function
- `invar` is the input argument
- `outvar` is the output argument, returned by the function

Examples :

```
--> y = sin(1.8)
y =
    0.9738476

--> x = [0:0.1:1];

--> N = length(x)
N =
    11.
```

User can define its own functions

```
function [out1,out2,...] = myfunction(in1,in2,...)
```

*body of the function*

```
endfunction
```

- once the environment `function...endfunction` is executed `myfunction` is defined and loaded in Scilab
- after any change in the function, it must be reloaded to be taken into account
- files including functions generally have the extension “.sci”

Example 1 : calculation of the roots of a quadratic equation.

Define and load the function

```
function [x1,x2] = roots_equ2d(a,b,c)
// roots of ax^2 + bx + c = 0
delta = b^2 - 4*a*c
x1 = (-b - sqrt(delta))/(2*a)
x2 = (-b + sqrt(delta))/(2*a)
endfunction
```

Then, you can use it as any other Scilab function

```
--> [r1,r2] = roots_equ2d(1,3,2)
r2 =
- 1.

r1 =
- 2.
```

Example 2 : functions are appropriate to define mathematical functions.

$$f(x) = (x + 1) e^{-2x}$$

```
function y = f(x)
    y = (x+1).*exp(-2*x);
endfunction
```

```
--> y = f(4)
y =
    0.0016773

--> y = f(2.5)
y =
    0.0235828

--> t = [0:0.1:5];

--> plot(t,f)
```

- Variables from workspace are known inside the function
- but any change inside the function remain local.

```
function z=mytest(x)
    z = x + a;
    a = a +1;
endfunction
```

```
--> a = 2;
--> mytest(3)
ans =
    5.

--> a
a =
    2.
```

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## For MATLAB users

Many instructions have the same syntax, but some others not...

A dictionary gives a list of the main MATLAB functions with their Scilab equivalents

[http://help.scilab.org/docs/5.4.1/en\\_US/section\\_36184e52ee88ad558380be4e92d3de21.html](http://help.scilab.org/docs/5.4.1/en_US/section_36184e52ee88ad558380be4e92d3de21.html)

Some tools are provided to convert MATLAB files to Scilab (e.g. `mfile2sci`)

[http://help.scilab.org/docs/5.4.1/en\\_US/About\\_M2SCI\\_tools.html](http://help.scilab.org/docs/5.4.1/en_US/About_M2SCI_tools.html)

A good note on Scilab for MATLAB users

Eike Rietsch, *An Introduction to Scilab from a Matlab User's Point of View*, May 2010

<http://www.scilab.org/en/resources/documentation/community>

## Somme differences about the syntax

### In MATLAB

- search with keywords `lookfor`
- comments `%`
- predefined constants `i`, `pi`, `inf`, `true`
- special characters in name of variables  
-  
● continuation of a statement `...`
- flow control `switch case otherwise`
- last element of a vector `x(end)`

### In Scilab

- search with keywords `apropos`
- comments `//`
- predefined constants `%i`, `%pi`, `%inf`, `%t`
- special characters in name of variables  
-, #, !, ?, \$  
● continuation of a statement `..`
- flow control `select case else`
- last element of a vector `x($)`

## Different responses for a same command

### In MATLAB

- **length**, the larger of the number of rows and columns
- after a first **plot**, a second one clears the current figure
- division by a vector  

```
>> x = 1/[1 2 3]
Error using / Matrix dimensions must agree.
```
- operators **==** and **~=** compare elements  

```
>> [1 2 3] == 1
ans =
1 0 0
>> [1 2 3] == [1 2]
Error using ==
Matrix dimensions must agree.
>> [1 2] == ['1','2']
ans =
0 0
```

### In Scilab

- **length**, the product of the number of rows and columns
- after a first **plot**, a second one holds the previous
- division by a vector  

```
--> x = 1/[1 2 3]
x =
0.0714286
0.1428571
0.2142857
x is solution of [1 2 3]*x = 1
```
- operators **==** and **~=** compare objects  

```
--> [1 2 3] == 1
ans =
T F F
--> [1 2 3] == [1 2]
ans =
F
--> [1 2] == ['1','2']
ans =
F
```

## Different responses for a same command

## In MATLAB

- for a matrix  $A=[1\ 2\ 4;4\ 8\ 2;6\ 0\ 9]$   
`>> max(A)`  
ans =  
7 8 9  
`>> sum(A)`  
ans =  
12 10 18
- `disp` must have a single argument  
`>> a=3;`  
`>> disp(['the result is',int2str(a),' ...bye!'])`  
  
the result is 3 ...bye!

## In Scilab

- for a matrix  $A=[1\ 2\ 4;4\ 8\ 2;6\ 0\ 9]$   
`--> max(A)`  
ans =  
9.  
`--> sum(A)`  
ans =  
36.
- `disp` may have several arguments  
`--> a = 3;`  
`--> disp(a,'the result is ' + string(a),'hello!')`  
  
hello!  
the result is 3  
3.
- note that : `prettyprint` generates the Latex code to represent a Scilab object

## Difference when running a script

### In MATLAB

- script is invoked by typing its name `myscript`
- the m-file must be in a directory of the search path (or specify the path in the call)
- use a semi-colon to print or not the result of an instruction

### In Scilab

- script is invoked with the `exec` command  
`--> exec('myscript.sce')`
- the file must be the working directory (or specify the path in the call)
- a second argument may be appended (mode) to specify what to print
- it does not seem to do what the documentation says... not clear for me

a simple example, *myscript.sce* :

```
// a simple script: myscript
a = 1
b = a+3;
disp('result is ' + string(b))
```

the second argument *mode*

Value	Meaning
0	the default value
-1	print nothing
1	echo each command line
2	print prompt -- >
3	echo + prompt
4	stop before each prompt
7	stop + prompt + echo

```
--> exec('myscript.sce',0)
a =

    1.

result is 4
```

(as Matlab works)

```
--> exec('myscript.sce',-1)

result is 4
```

(only output of disp is printed)

```
--> exec('myscript.sce',1)
--> // a simple script: myscript
--> a = 1
a =

    1.
--> b = a+3;
--> disp('result is ' + string(b))

result is 4
```

(everything is printed (instructions and outputs))



## Difference when using user defined functions

### In MATLAB

- a function is a file, they must have the same name
- variables in the function are local variables
- any other functions defined in the file are local functions

### In Scilab

- a function is a variable
- variables in the function are local variables and variables from the calling workspace are known
- when defined (`function ... endfunction`), functions are not executed but loaded
- any change in the function requires to reload it (executing the environment)

A function may be defined directly in the console :

```
-->
-->function [y] = addition(u1,u2)
-->     y = u1 + u2;
-->endfunction
-->
--> addition(2,3)
ans =

     5.
```

or in a file `anyscript.sce`, and the file must be executed :

```
--> addition(2,3)
           !--error 4
Variable non définie : addition

--> exec('anyscript.sce', -1)
--> addition(2,3)
ans =

     5.
```

Any change needs to redefine (reload) the function to be taken into account.

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# Exercices

## Exercise 1

Calculate the sum of the first 100 integers squared,

$$1 + 2^2 + 3^2 + 4^2 + \dots + 100^2$$

in 3 different ways :

- with instruction `for`,
- with instruction `while`,
- with instruction `sum`.

## Exercise 2

Let us consider a monotonic increasing function  $f$  over an interval  $[a, b]$  such that

$$f(a) < 0 \quad \text{and} \quad f(b) > 0$$

Write an algorithm, based on a dichotomic search, to find the root  $x_0$  such that  $f(x_0) = 0$ .

- $f_1(x) = 2x^4 + 2.3x^3 - 16x^2 - 8x - 17.5$  with  $x \in [0, 100]$ ,
- $f_2(x) = \tan(x^2) - x$  with  $x \in [0.5, \pi/3]$ .

### Exercise 3

The Fourier expansion of a square wave  $f$  with a period  $T$  and an amplitude  $A$  is of the form :

$$f(t) = \sum_{n=1}^{+\infty} a_n \cos(n\omega t) \quad \text{with} \quad a_n = \frac{2A}{n\pi} \sin\left(n\frac{\pi}{2}\right) \quad \text{and} \quad \omega = \frac{2\pi}{T}.$$

Plot the Fourier expansion for different numbers of harmonics.

numerical values :  $A = 2$ ,  $T = 0.5s$ ,  $t \in [0, 2]$ .

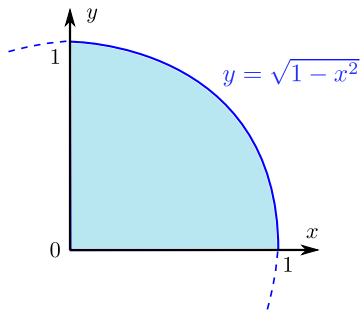
## Exercise 4

Numerical integration for estimating  $\pi$

$\pi$  = surface of a unit disc

$$x^2 + y^2 = 1$$

Compute the area of a quarter of the disc with the rectangle method.



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# Xcos

Xcos is a graphical environment to simulate dynamic systems.

It is the Simulink<sup>®</sup> counterpart of Scilab.

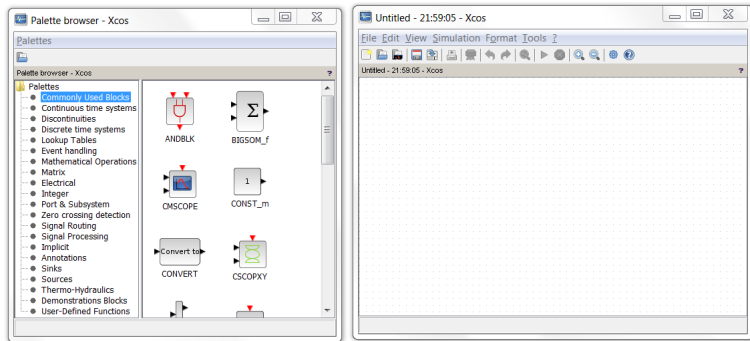
It is launched in *Application/Xcos* or by typing `xcos`

# Xcos

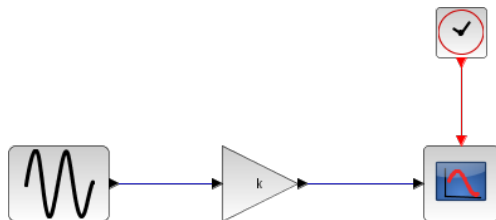
Xcos is a graphical environment to simulate dynamic systems.

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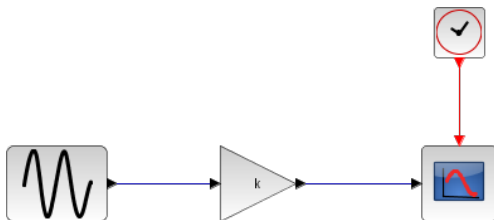
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## A simple example



## A simple example

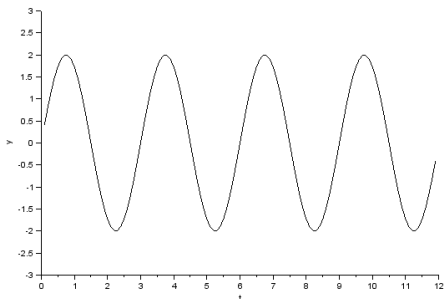


block	sub-palette
sinus	Sources/GENSIN_f
gain	Math. Operations/GAINBLK_f
scope	Sinks/CSCOPE
clock	Sources/CLOCK_c

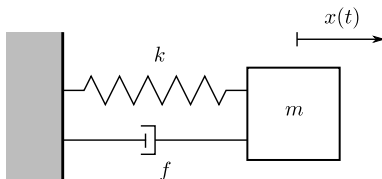
- drag and drop blocks from the palette browser to the editing window
- $k$  is variable from the workspace (or from Simulation/Set context)
- black lines are data flows and red lines are event flows

Settings : frequency =  $2\pi/3$ ,  $k = 2$ , final integral time = 12,  $Y_{\min} = -3$ ,  $Y_{\max} = 3$ , Refresh period = 12

Run simulation from Simulation/Start



Let simulate a mass-spring-damper system

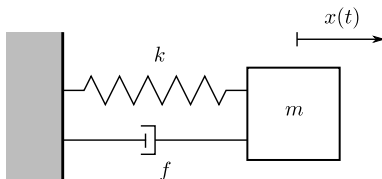


The system can be described by the equation of motion

$$m\ddot{x}(t) + f\dot{x}(t) + kx(t) = 0$$

with the initial conditions :  $x(0) = 5$  and  $\dot{x}(0) = 0$

Let simulate a mass-spring-damper system



The system can be described by the equation of motion

$$m\ddot{x}(t) + f\dot{x}(t) + kx(t) = 0$$

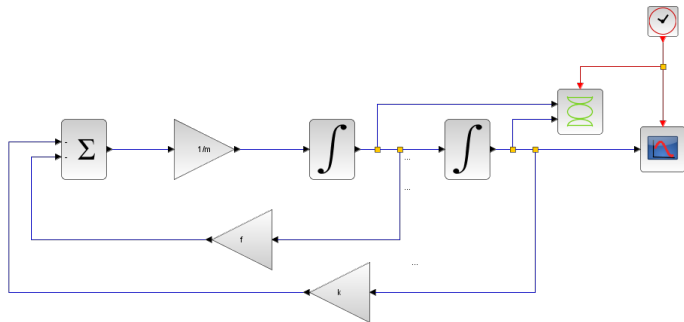
with the initial conditions :  $x(0) = 5$  and  $\dot{x}(0) = 0$

The acceleration of the mass is then given by

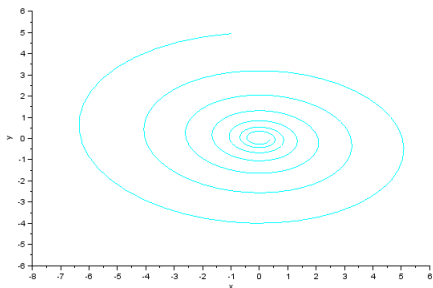
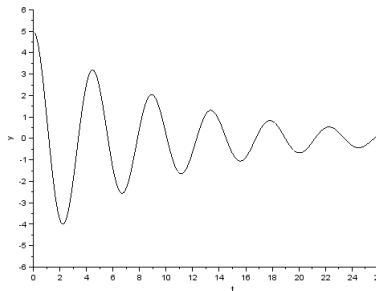
$$\ddot{x}(t) = -\frac{1}{m} \left( kx(t) + f\dot{x}(t) \right)$$



## modeling and simulation with Xcos



block	sub-palette
sum	Math. Operations/BIGSOM_f
gain	Math. Operations/GAINBLK_f
integral	Cont. time systems/INTEGRAL_m
scope	Sinks/CSCOPE
x-y scope	Sinks/CSCOPXY
clock	Sources/CLOCK_c

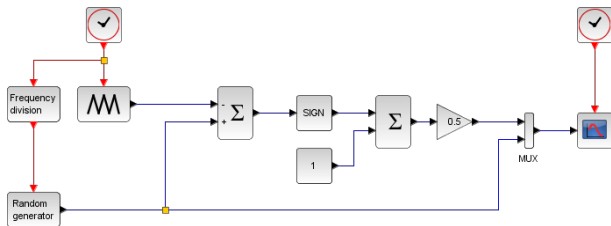


parameters :  $m = 1$ ,  $k = 2$  and  $f = 0.2$

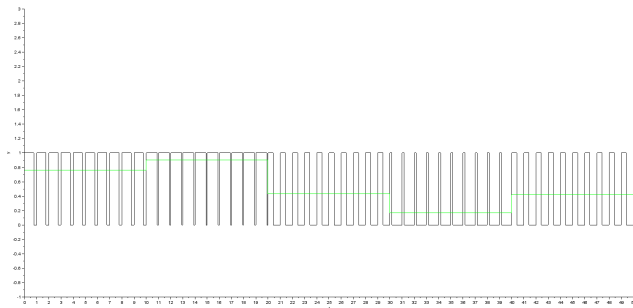
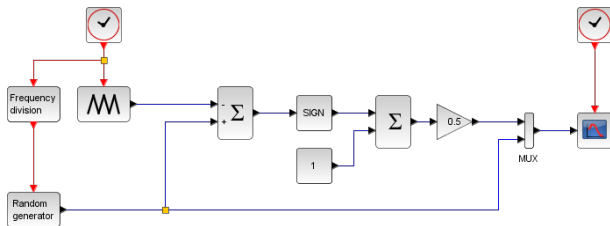




## Example 3 : simulation of a PWM signal



### Example 3 : simulation of a PWM signal



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# Physical modeling

Xcos includes, as a module extension, Modelica blocks.

It provides a physical approach for modeling



# Physical modeling

Xcos includes, as a module extension, Modelica blocks.

It provides a physical approach for modeling

physical modeling  
or  
acausal modeling

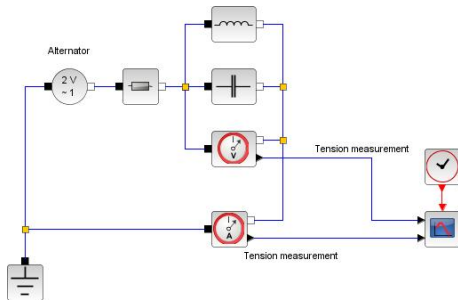
≠

causal modeling  
with  
input/output relations

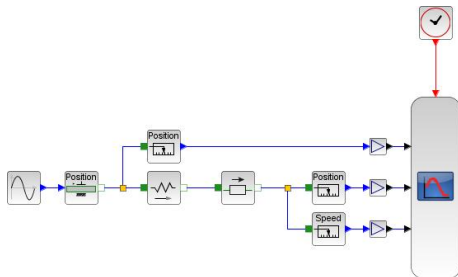
Modelica blocks in Xcos require a C compiler

## Examples

### Electrical system



### Mechanical system

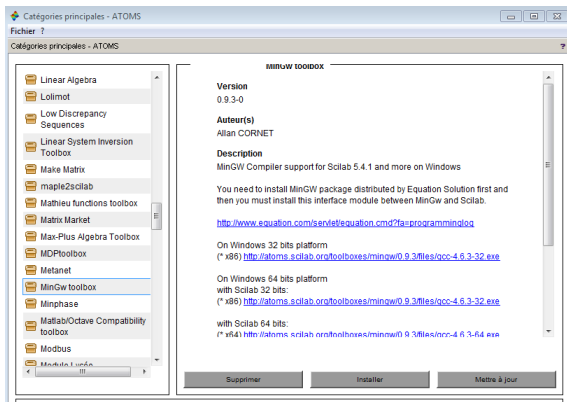


## Installation requirements :

- install a gcc compiler (in the OS),
- install MinGW toolbox (in Scilab),
- install Coselica Toolbox for more Modelica blocks (in Scilab, optional)

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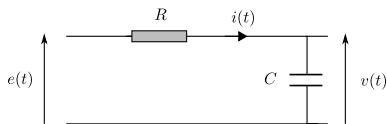
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# Exercices

## Exercise 1

Let us consider a RC circuit



The system can be described by the linear differential equation

$$RC\dot{v}(t) + v(t) = e(t)$$

with the initial condition :  $v(0) = 0$ .

Simulate the response  $v(t)$  to a step input  $e(t) = 5V$ .

## Exercise 2

Let us consider the predator-prey model based on Lotka-Volterra equations

$$\begin{cases} \dot{x}(t) &= x(t) \left( a - by(t) \right) \\ \dot{y}(t) &= y(t) \left( -c + dx(t) \right) \end{cases}$$

where

- $x(t)$  is the number of prey
- $y(t)$  is the number of predator
- $a$  and  $d$  are parameters describing the growth of the prey population and the predator population
- $b$  and  $c$  are parameters describing the death rate of the prey population and the predator population

Simulate<sup>2</sup> the evolution of populations with initial conditions  $x(0) = 4$  and  $y(0) = 2$ .

---

2. numerical values :  $a = 3$ ,  $b = 1$ ,  $c = 2$ ,  $d = 1$

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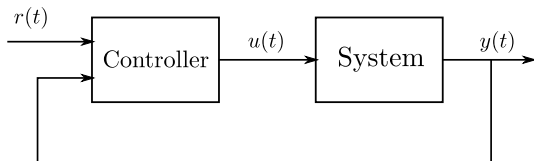
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## A brief review

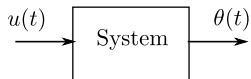
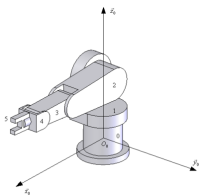
**Objective :** Design a controller to control a dynamical system.



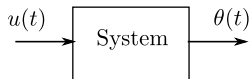
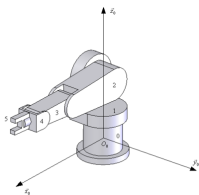
The output to be controlled is measured and taken into account by the controller.

$\Rightarrow$  feedback control

**Example :** angular position control of a robotic arm.



**Example :** angular position control of a robotic arm.



- $u(t)$  is the control voltage of the DC motor (actuator)
- $\theta(t)$  is the angular position of the arm (measured with a sensor)

The input-output relationship is given by :

$$\ddot{\theta}(t) + \dot{\theta}(t) = u(t)$$

The corresponding transfer function is

$$G(s) = \frac{\hat{\theta}(s)}{\hat{u}(s)} = \frac{1}{(s+1)s}$$

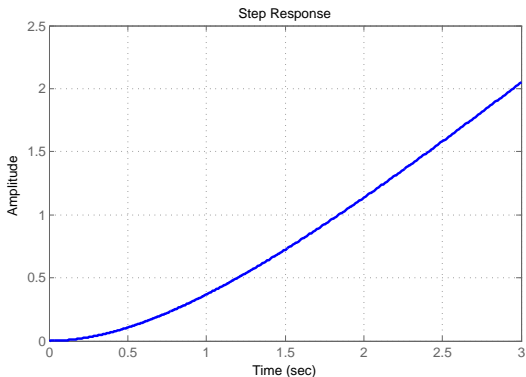
It has 2 poles :  $-1$  and  $0 \Rightarrow$  system is unstable

The corresponding transfer function is

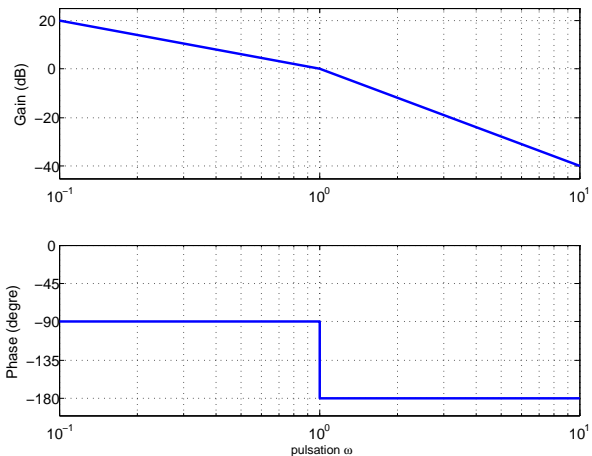
$$G(s) = \frac{\hat{\theta}(s)}{\hat{u}(s)} = \frac{1}{(s+1)s}$$

It has 2 poles :  $-1$  and  $0 \Rightarrow$  system is unstable

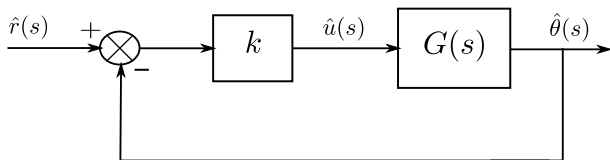
Its step response is divergent



The asymptotic bode diagram :

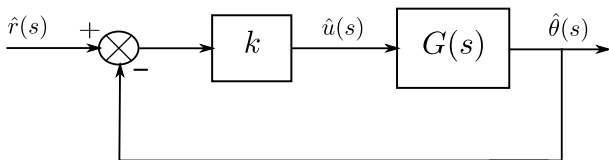


Closed-loop control with a proportional gain  $k$





Closed-loop control with a proportional gain  $k$

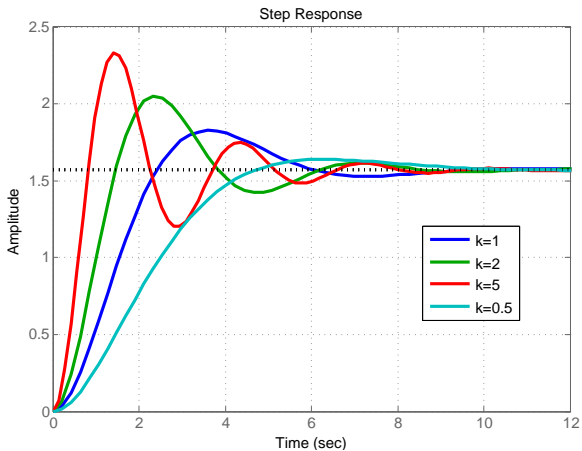


The closed-loop transfer function is

$$F(s) = \frac{k}{s^2 + s + k}$$

The Routh criterion shows that  $F(s)$  is stable  $\forall k > 0$ .

Response of  $\theta(t)$  for a step reference  $r(t) = \frac{\pi}{2}$



## Quick analysis of the feedback system

The tracking error is given by :  $\varepsilon(t) = r(t) - \theta(t)$

$$\hat{\varepsilon}(s) = \frac{s^2 + s}{s^2 + s + k} \hat{r}(s)$$

the static error is zero :  $\varepsilon_s = \lim_{s \rightarrow 0} s \hat{\varepsilon}(s) = 0$  (with  $\hat{r}(s) = \frac{\pi/2}{s}$ )

## Quick analysis of the feedback system

The tracking error is given by :  $\varepsilon(t) = r(t) - \theta(t)$

$$\hat{\varepsilon}(s) = \frac{s^2 + s}{s^2 + s + k} \hat{r}(s)$$

the static error is zero :  $\varepsilon_s = \lim_{s \rightarrow 0} s \hat{\varepsilon}(s) = 0$  (with  $\hat{r}(s) = \frac{\pi/2}{s}$ )

Using the standard form of 2<sup>nd</sup> order systems :

$$F(s) = \frac{K\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \quad \Rightarrow \quad \begin{cases} K & = & 1, \\ \omega_n & = & \sqrt{k} \\ \zeta & = & 1/2\sqrt{k} \end{cases}$$

we can conclude that

- when  $k \nearrow$ , damping  $\zeta \searrow$  and oscillations  $\nearrow$
- settling time  $t_{5\%} \approx \frac{3}{\zeta\omega_n} = 6s$ .

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# System analysis in Scilab

## Definition of a transfer function

```
--> num = 1;
--> den = %s^2+%s;
--> G = syslin('c',num,den)
G =

      1
-----
      2
     s + s

--> roots(den)
ans =

- 1.
  0
```

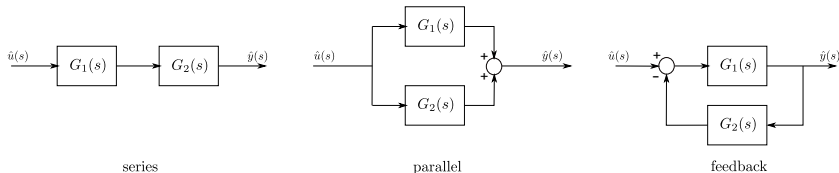
- The argument `c` stands for continuous-time system (`d` for discrete)
- The instruction `roots` is useful to calculate the poles of a transfer function
- The instruction `plzr` plots the pole-zero map in the complex plane

## Computation of the time response

```
--> t = [0:0.02:3];  
  
--> theta = csim('step',t,G);  
  
--> plot(t,theta)
```

- The string argument **step** is the control, it can be **impuls**, a vector or a function.
- To define the time vector, you may also use the **linspace** instruction.
- For frequency analysis, different instructions are provided : **repfreq**, **bode**, **nyquist**, **black**.

## Systems connection



The mathematical operators can handle `syslin` type

Example

$$G_1(s) = \frac{1}{s+2} \quad \text{and} \quad G_2(s) = \frac{4}{s}$$

```
--> G1 = syslin('c',1,%s+2);
--> G2 = syslin('c',4,%s);
```



```

--> G1 * G2      // series connection
ans  =
      4
-----
      2
    2s + s

--> G1 + G2      // parallel connection
ans  =
    8 + 5s
-----
      2
    2s + s

--> G1 /. G2     // feedback connection
ans  =
      s
-----
      2
    4 + 2s + s

```

## Back to our case study

Let simulate the closed-loop control with a proportional gain

```
--> k = 2;
--> F = (G*k) /. 1
F =
      2
-----
      2
2 + s + s

--> routh_t(%s^2+%s+2)
ans =

      1.      2.
      1.      0.
      2.      0.

--> [wn, zeta] = damp(F)
zeta =
      0.3535534
      0.3535534
wn =
      1.4142136
      1.4142136

--> t = linspace(0,12,200);
--> theta = csim('step',t,F)*%pi/2;
--> plot(t,theta)
```

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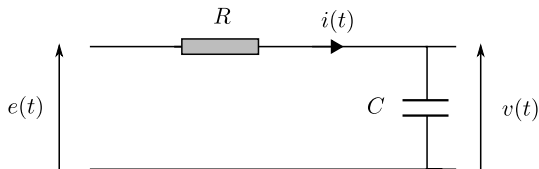
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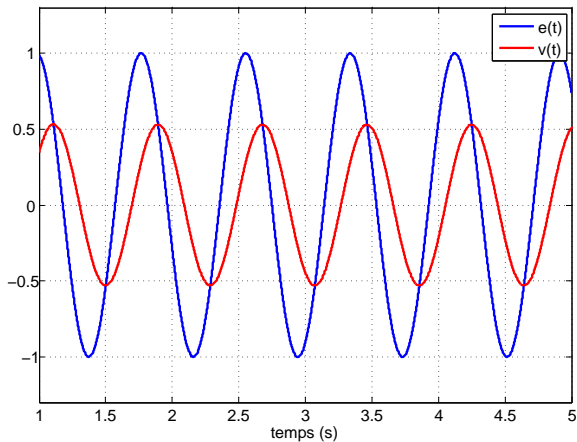
# Bode plot

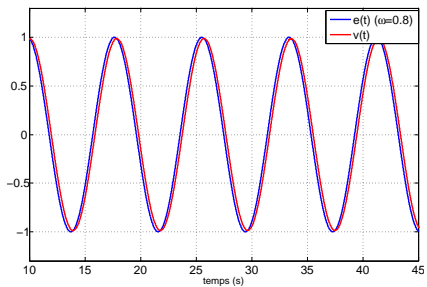
Introductory example : RC circuit

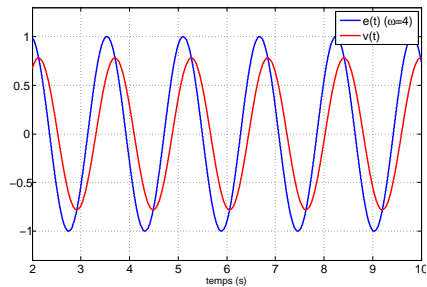
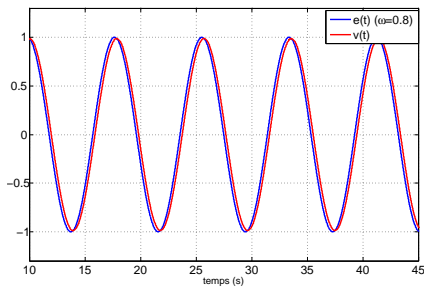




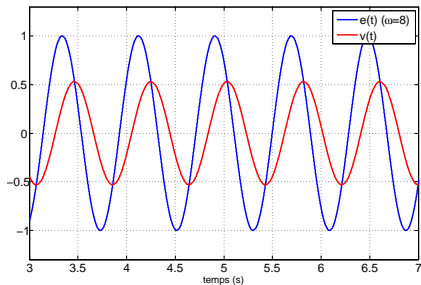
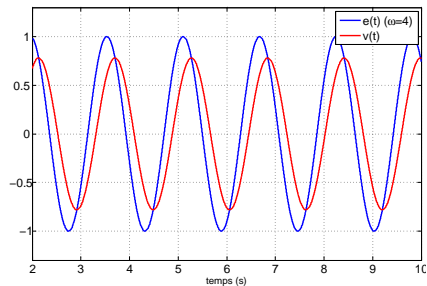
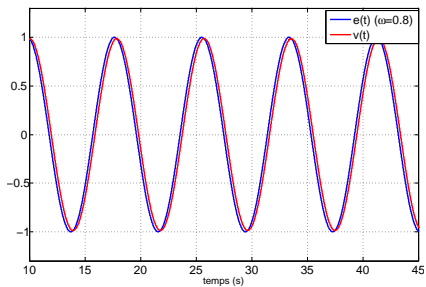
For  $R = 1k\Omega$  and  $C = 200\mu F$ , let apply a voltage  $e(t) = \cos(8t)$ .

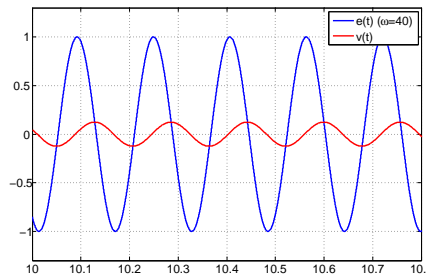
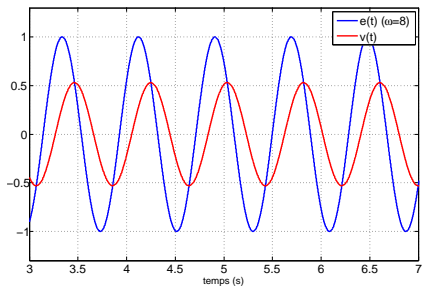
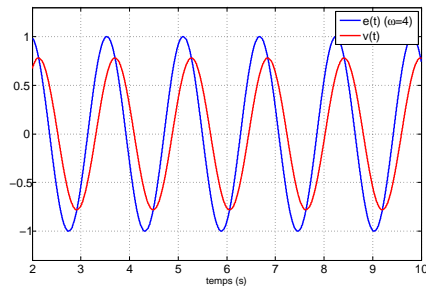
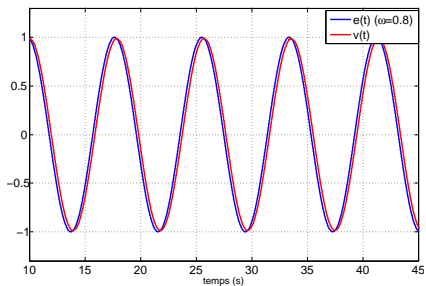


Responses of the circuit with  $\omega = \{0.8, 4, 8, 40\}$ 

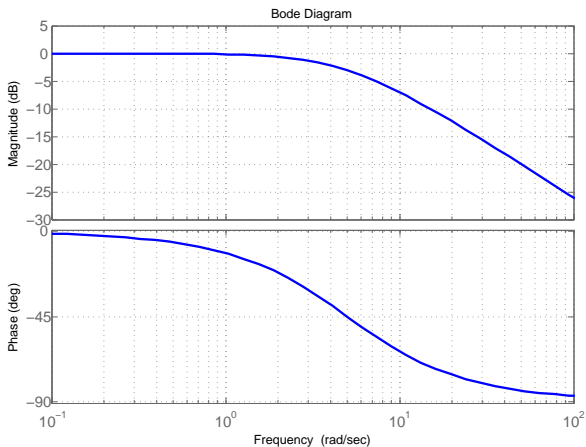
Responses of the circuit with  $\omega = \{0.8, 4, 8, 40\}$ 



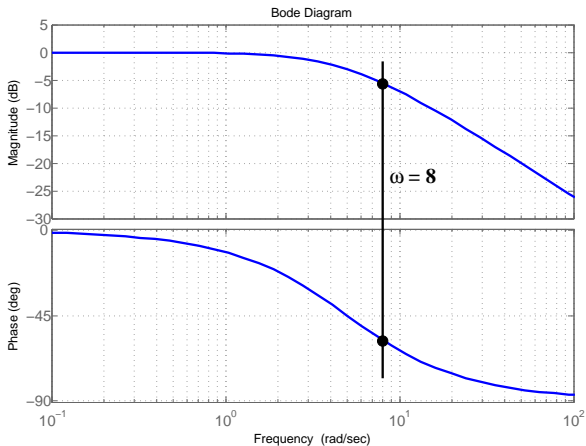
Responses of the circuit with  $\omega = \{0.8, 4, 8, 40\}$ 

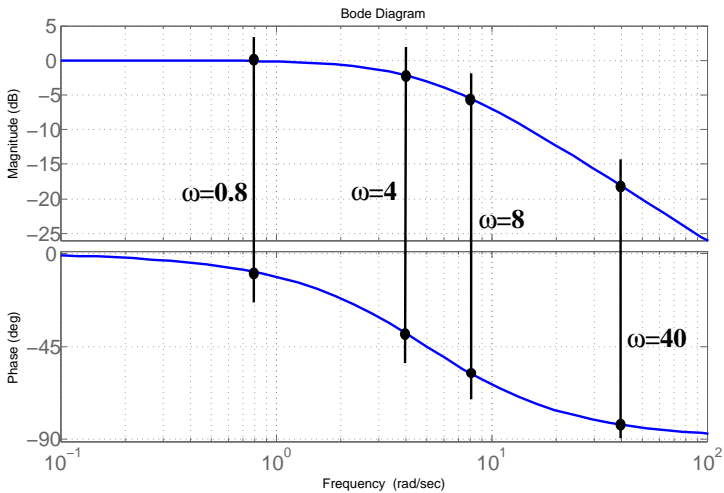
Responses of the circuit with  $\omega = \{0.8, 4, 8, 40\}$ 

## Bode diagram of the transfer function

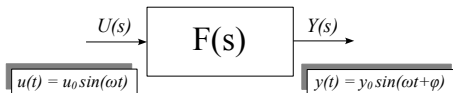


## Bode diagram of the transfer function

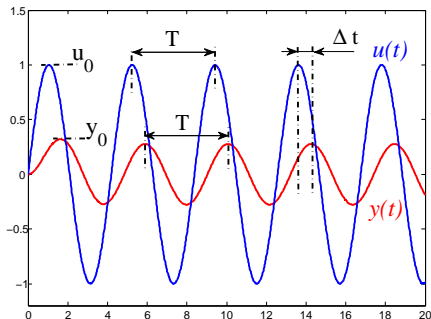
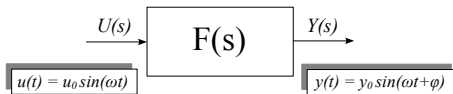




Frequency analysis consists in studying the response of a LTI system with sine inputs



Frequency analysis consists in studying the response of a LTI system with sine inputs



The output signal is also a sine with the same frequency, but with a different magnitude and a different phase angle.

A system can then be characterized by its

- gain :  $\frac{y_0}{u_0}$
- phase shift :  $\pm 360 \frac{\Delta t}{T}$

The magnitude and the phase depend on the frequency  $\omega$



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- gain :  $\frac{y_0}{u_0}$
- phase shift :  $\pm 360 \frac{\Delta t}{T}$

The magnitude and the phase depend on the frequency  $\omega$

It can be shown that :

- gain =  $|F(j\omega)|$ ,
- phase shift =  $\arg F(j\omega)$ .

$F(j\omega)$  is the transfer function of the system where the Laplace variable  $s$  has been replaced by  $j\omega$ .

Example : let consider system

$$F(s) = \frac{1/2}{s + 1}$$

What are the responses to these inputs ?

$$u_1 = \sin(0.05 t)$$

$$u_2 = \sin(1.5 t)$$

$$u_3 = \sin(10 t)$$

Example : let consider system

$$F(s) = \frac{1/2}{s + 1}$$

What are the responses to these inputs ?

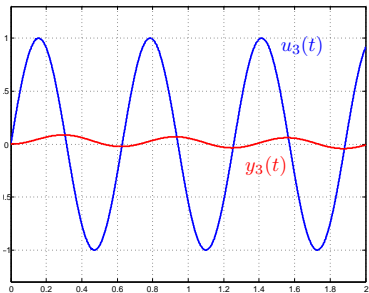
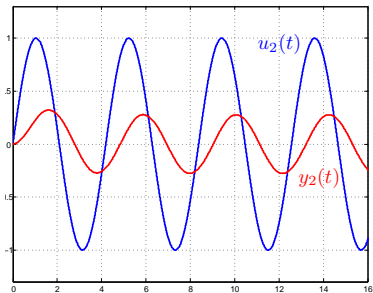
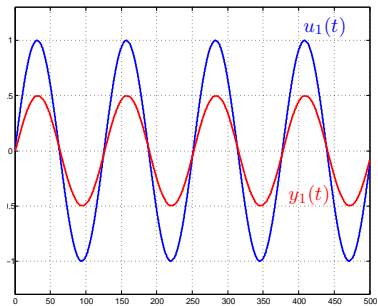
$$u_1 = \sin(0.05 t)$$

$$u_2 = \sin(1.5 t)$$

$$u_3 = \sin(10 t)$$

we express  $F(j\omega) = \frac{1/2}{j\omega + 1}$

- for  $\omega = 0.05 \text{ rad/s}$  :  $|F(j0.05)| = 0.5$  and  $\arg F(j0.05) = -2.86^\circ$ .
- for  $\omega = 1.5 \text{ rad/s}$  :  $|F(j1.5)| = 0.277$  and  $\arg F(j1.5) = -56.3^\circ$ .
- for  $\omega = 10 \text{ rad/s}$  :  $|F(j10)| = 0.05$  and  $\arg F(j10) = -84.3^\circ$ .

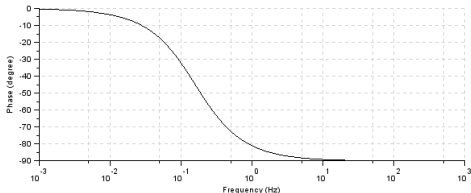
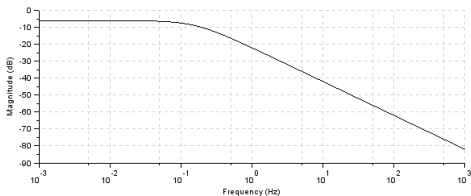


**Bode diagram** : it plots the gain and the phase shift w.r.t. the frequency  $\omega$

- the gain is expressed as decibels : gain dB =  $20 \log \frac{y_0}{u_0}$
- property : the Bode diagram of  $F(s)G(s)$  is the sum of the one of  $F(s)$  and the one of  $G(s)$ .
- in Scilab, the instruction `bode(F)` plots the Bode diagram of  $F(s)$ .

**Bode diagram** : it plots the gain and the phase shift w.r.t. the frequency  $\omega$

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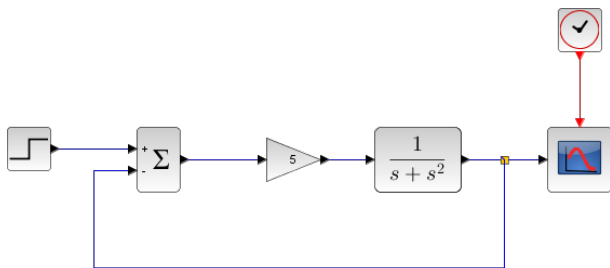
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## Simulation with Xcos

Let simulate the closed-loop control with a proportional gain

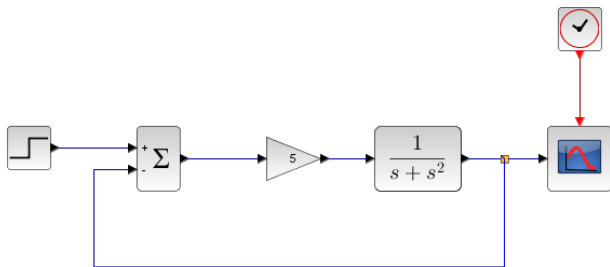


...



## Simulation with Xcos

Let simulate the closed-loop control with a proportional gain



block	sub-palette
step	Sources/STEP_FUNCTION
sum	Math. Operations/BIGSOM_f
gain	Math. Operations/GAINBLK_f
transfert function	Cont. time systems/CLR
scope	Sinks/CSCOPE
clock	Sources/CLOCK_c

settings : final value (step) =  $\%pi/2$ , final integral time = 12, Ymin= 0, Ymax= 2.5, Refresh period = 12

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# Exercices

Let us consider a system modeled by

$$G(s) = \frac{4}{4s^2 + 4s + 5}$$

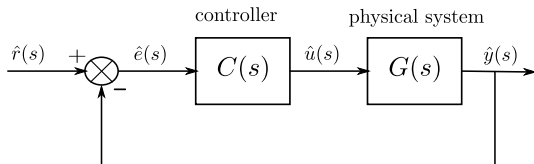
- Calculate poles. Is the system stable?
- Calculate the closed-loop transfer function (with a proportional gain  $k$ ).
- Calculate the minimal value of  $k$  to have a static error  $\geq 10\%$ .
- Calculate the maximal value of  $k$  to have an overshoot  $\leq 30\%$ .
- Simulate all these cases with Xcos.

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## Classical control design

Control design aims at designing a controller  $C(s)$  in order to assign desired performances to the closed loop system



- Classical control is a frequency domain approach and is essentially based on Bode plot
- Main controllers, or compensators, are phase lag, phase lead, PID (proportional integral derivative)

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# Loopshaping

Let express the tracking error

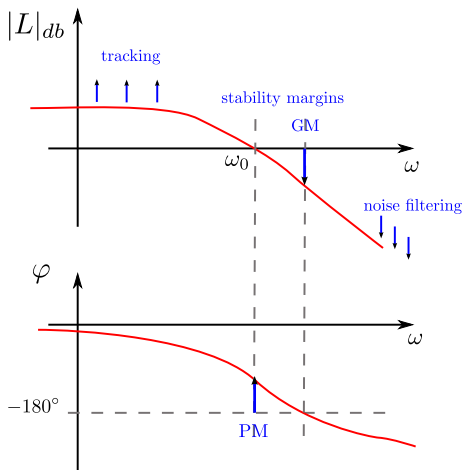
$$\hat{e}(s) = \frac{1}{1 + G(s)C(s)} \hat{r}(s)$$

So, a high open-loop gain results in a good tracking

- it leads to better accuracy and faster response (depending on the bandwidth)
- but it leads to a more aggressive control input ( $u$ )
- but it reduces stability margins

Let define the open-loop transfer function  $L = GC$

Closed-loop performances can be assessed from the Bode plot of  $L$



- PM and GM are phase and gain margins
- noise disturbances are a high frequency signals



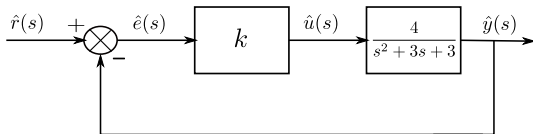
Loopshaping consists in designing the controller  $C(s)$  so as to “shape” the frequency response of  $L(s)$

we recall that

$$|L|_{db} = |GC|_{db} = |G|_{db} + |C|_{db}$$

The desired “shape” depends on performance requirements for the closed-loop system

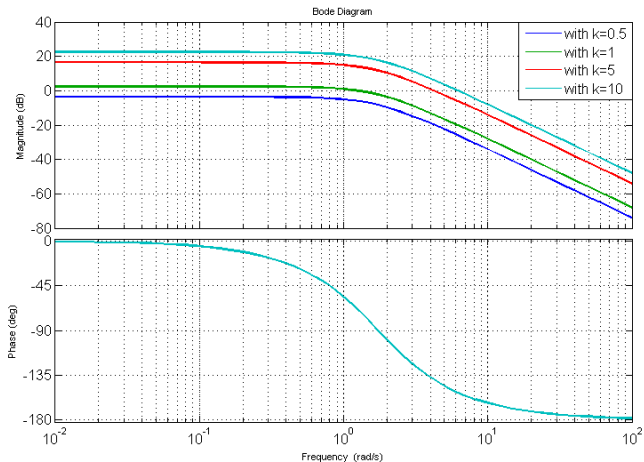
A simple example with a proportional controller



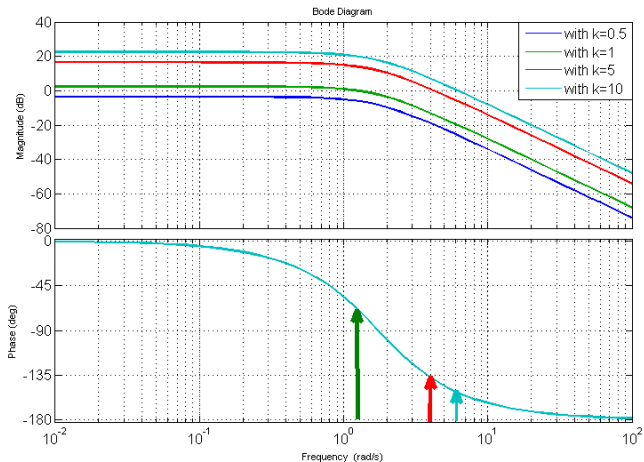
The open-loop transfer function is

$$L(s) = \frac{4k}{s^2 + 3s + 3}$$

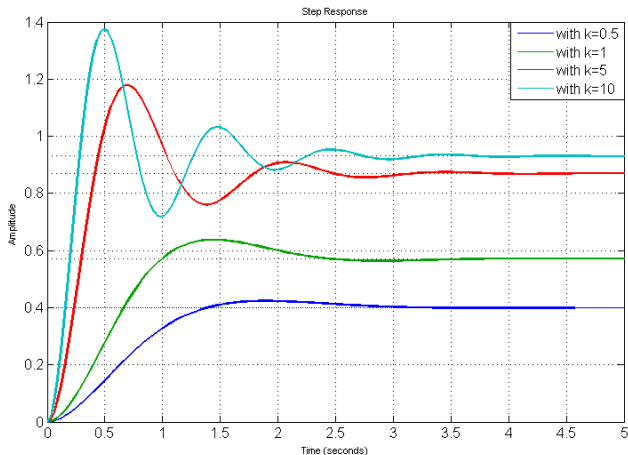
Bode plot of  $L(s)$  for  $k = \{0.5, 1, 5, 10\}$



Bode plot of  $L(s)$  for  $k = \{0.5, 1, 5, 10\}$



when  $k$  increases, the phase margin decreases

Step response of the closed-loop system (unit step) for  $k = \{0.5, 1, 5, 10\}$ 

- the static error decreases as  $k$  increases
- oscillations increase as  $k$  increases

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## Phase lag controller

The transfer function of the phase lag controller is of the form

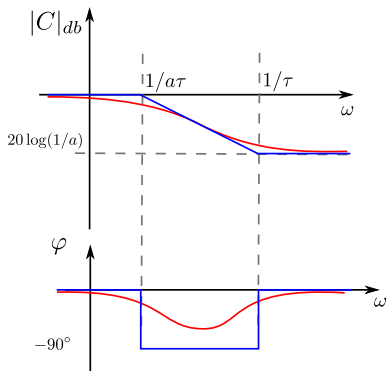
$$C(s) = \frac{1 + \tau s}{1 + a\tau s}, \quad \text{with } a > 1$$

## Phase lag controller

The transfer function of the phase lag controller is of the form

$$C(s) = \frac{1 + \tau s}{1 + a\tau s}, \quad \text{with } a > 1$$

- $a$  and  $\tau$  are tuning parameters
- It allows a higher gain in low frequencies
- But the phase lag must not reduce the phase margin





## Example

$$G(s) = \frac{4}{s^2 + 3s + 3}$$

What value for the proportional gain  $k$  to have a static error of 10%?

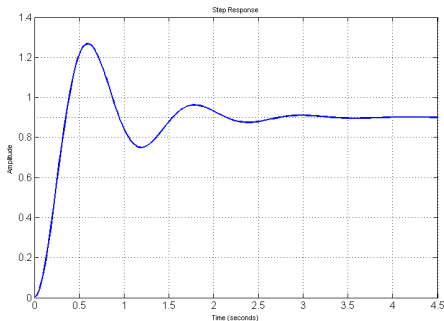
## Example

$$G(s) = \frac{4}{s^2 + 3s + 3}$$

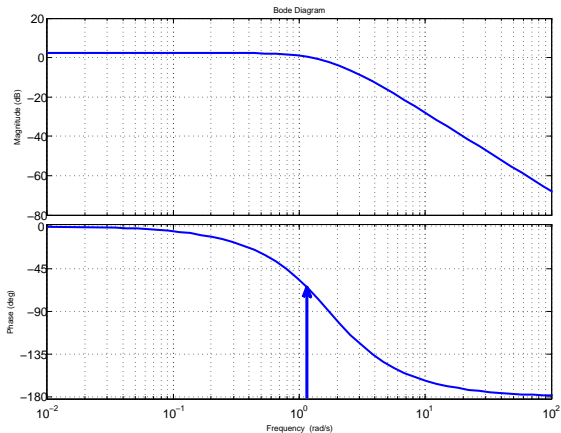
What value for the proportional gain  $k$  to have a static error of 10%?

$$\text{static error} = \frac{1}{1 + \frac{4}{3}k} = 0.1 \quad \Rightarrow \quad k = 6.75$$

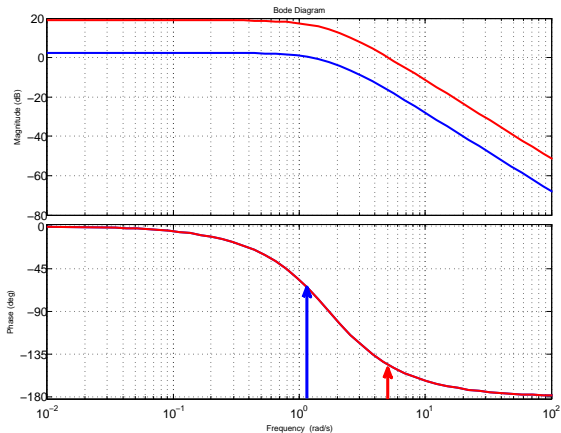
close-loop system response



Precision ok, but too much oscillations



Precision ok, but too much oscillations

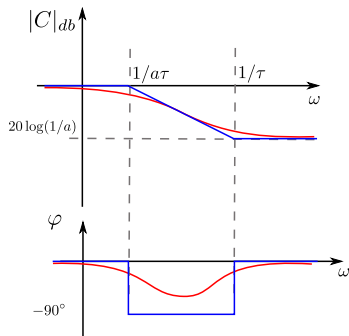


Phase margin : before =  $111^\circ$  (at  $1.24 \text{ rd/s}$ ); after =  $34^\circ$  (at  $5.04 \text{ rd/s}$ )

Phase lag controller

$$C(s) = \frac{1 + \tau s}{1 + a\tau s}$$

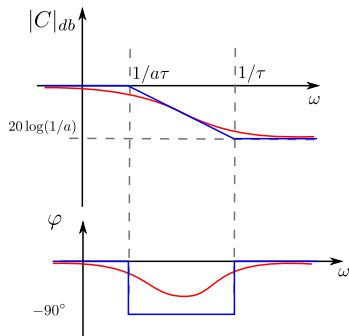
with  $a > 1$



Phase lag controller

$$C(s) = \frac{1 + \tau s}{1 + a\tau s}$$

with  $a > 1$

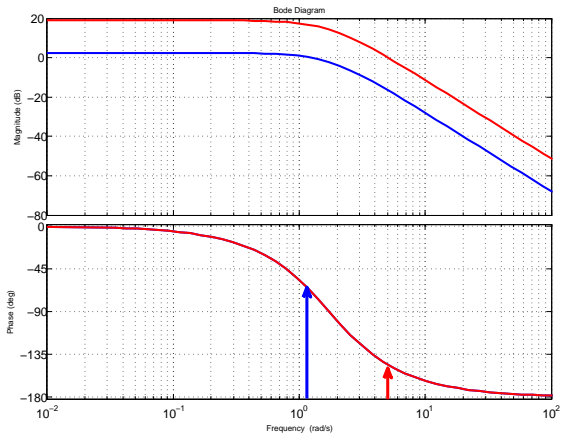


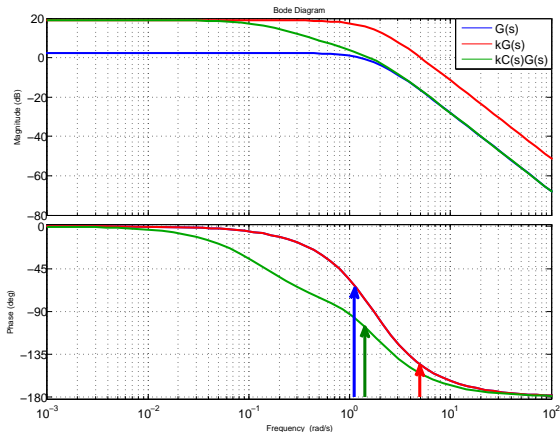
- We want a high gain only at low frequencies
- Phase lag must occur before the crossover frequency

$$\frac{1}{\tau} < \omega_0 = 1.24 \quad \Rightarrow \quad \tau = 1$$

- Then, we want to recover a gain of 1

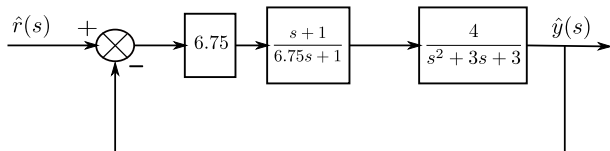
$$a = 6.75$$

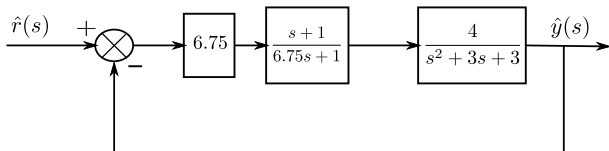




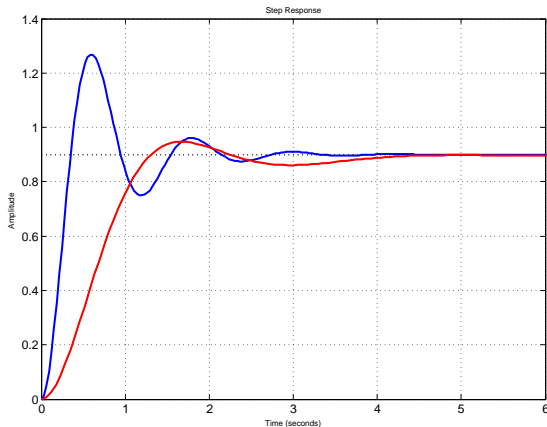
Phase margin : now, with the proportional gain and the phase lag controller  
 $= 70^\circ$  (at  $1.56 \text{ rd/s}$ )







close-loop system response



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  - **Phase lead controller**
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## Phase lead controller

The transfer function of the phase lead controller is of the form

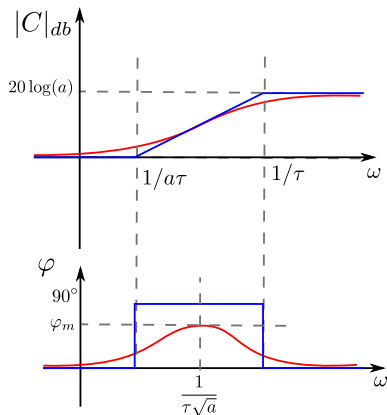
$$C(s) = \frac{1 + a\tau s}{1 + \tau s}, \quad \text{with } a > 1$$

## Phase lead controller

The transfer function of the phase lead controller is of the form

$$C(s) = \frac{1 + a\tau s}{1 + \tau s}, \quad \text{with } a > 1$$

- $a$  and  $\tau$  are tuning parameters
- It provides a phase lead in a frequency range
- But the gain may shift the crossover frequency



The phase lead compensator is used to increase the phase margin

Procedure :

- firstly, adjust a proportional gain  $k$  to reach a tradeoff between speed/accuracy and overshoot.
- measure the current phase margin and subtract to the desired margin

$$\varphi_m = PM_{\text{desired}} - PM_{\text{current}}$$

- compute  $a$

$$a = \frac{1 + \sin \varphi_m}{1 - \sin \varphi_m}$$

- at the maximum phase lead  $\varphi_m$ , the magnitude is  $20 \log \sqrt{a}$ . Find the frequency  $\omega_m$  for which the magnitude of  $kG(s)$  is  $-20 \log \sqrt{a}$

- compute  $\tau$

$$\tau = \frac{1}{\omega_m \sqrt{a}}$$

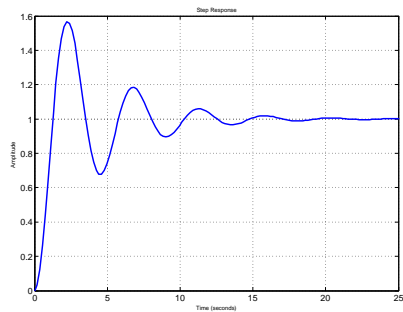
## Example

$$G(s) = \frac{4}{s(2s + 1)}$$

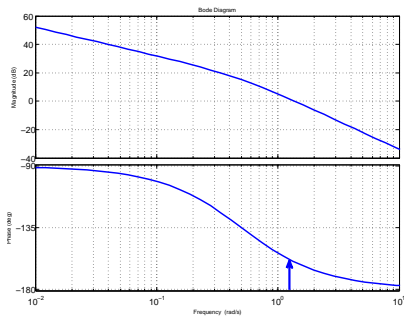
## Example

$$G(s) = \frac{4}{s(2s + 1)}$$

close-loop system response



open-loop bode diagram

Phase margin :  $20^\circ$  at  $1.37 \text{ rd/s}$



## Design of a phase lead compensator

- current phase margin is  $20^\circ$ , and the desired margin is, say,  $60^\circ$

$$\varphi_m = 40^\circ = 0.70 \text{ rd}$$

- compute  $a$

$$a = \frac{1 + \sin \varphi_m}{1 - \sin \varphi_m} = 4.62$$

- at the maximum phase lead  $\varphi_m$ , the magnitude is  $6.65 \text{ db}$ . At the frequency  $\sim 2 \text{ rd/s}$  the magnitude of  $G(s)$  is  $-6.65 \text{ db}$

- compute  $\tau$

$$\tau = \frac{1}{\omega_m \sqrt{a}} = 0.23$$

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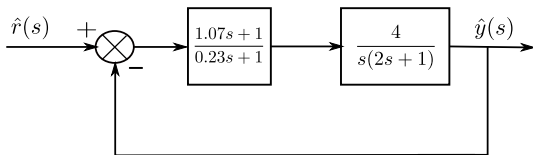
- compute  $\tau$

$$\tau = \frac{1}{\omega_m \sqrt{a}} = 0.23$$

Hence, the controller is of the form

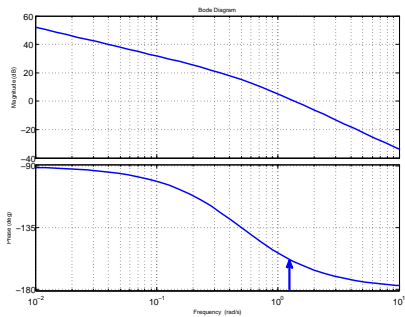
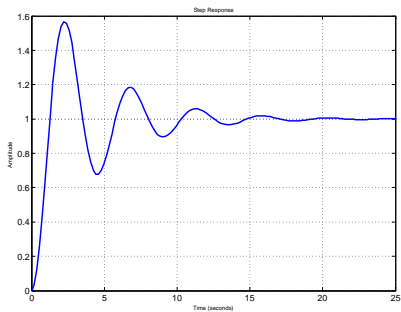
$$C(s) = \frac{1 + 1.07s}{1 + 0.23s}$$

## Example

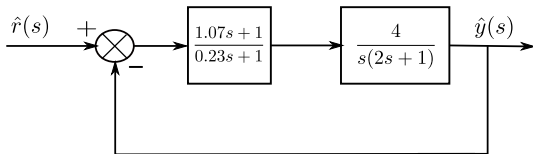


close-loop system response

open-loop bode diagram

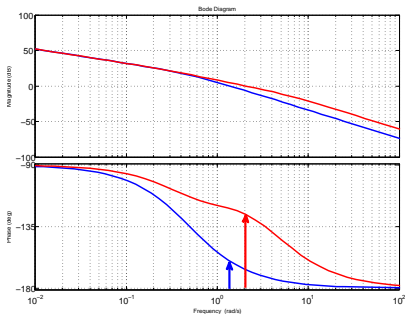
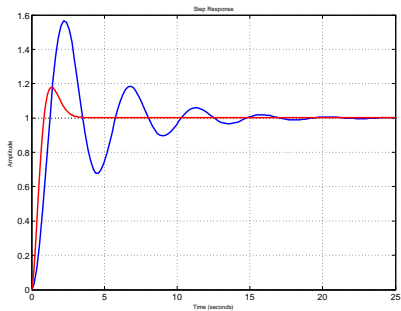


## Example



close-loop system response

open-loop bode diagram

New phase margin :  $53.7^\circ$  at  $2 \text{ rad/s}$

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# PID controller

A PID controller consists in 3 control actions

⇒ proportional, integral and derivative

Transfer function of the form :

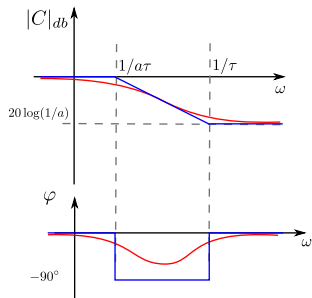
$$\begin{aligned} C(s) &= k_p + k_i \frac{1}{s} + k_d s \\ &= k_p \left(1 + \frac{1}{\tau_i s}\right) (1 + \tau_d s) \end{aligned}$$

The phase lag controller is an approximation of the PI controller

Phase lag controller

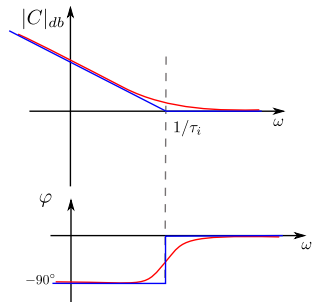
$$C(s) = \frac{1 + \tau s}{1 + a\tau s}$$

with  $a > 1$



PI controller

$$C(s) = \frac{1 + \tau_i s}{\tau_i s}$$

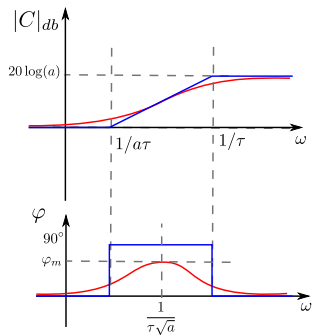


The phase lead controller is an approximation of the PD controller

Phase lead controller

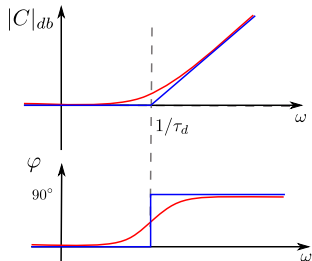
$$C(s) = \frac{1 + a\tau s}{1 + \tau s}$$

with  $a > 1$



PD controller

$$C(s) = 1 + \tau_d s$$





A PID controller is a combination of phase lag and phase lead controllers

$$C(s) = k \left( \frac{1 + \tau_1 s}{1 + a_1 \tau_1 s} \right) \left( \frac{1 + a_2 \tau_2 s}{1 + \tau_2 s} \right)$$

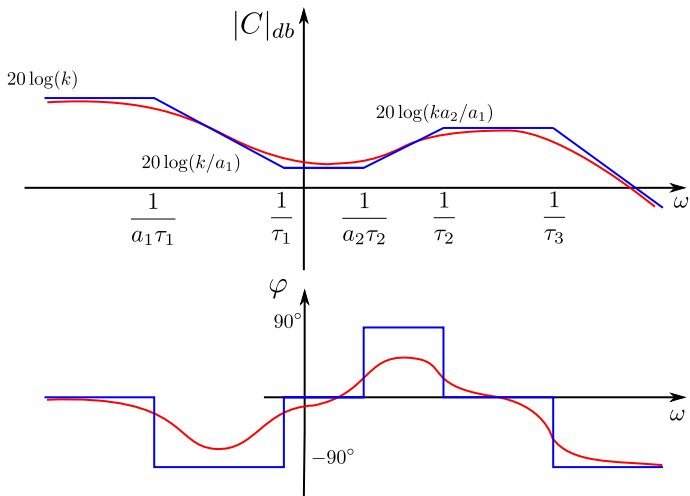
with  $a_1 > 1$  and  $a_2 > 1$ .

Transfer function of the form :

- the phase lag part is designed to improve accuracy and responsiveness
- the phase lead part is designed to improve stability margins
- an extra low-pass filter may be added to reduce noise

$$C_1(s) = \frac{1}{1 + \tau_3 s}$$

with  $\tau_3 \ll \tau_2$



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# Exercices

## Exercise 1

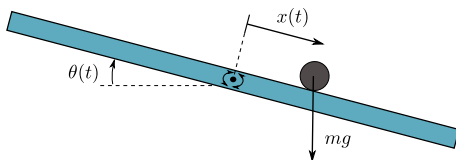
Let us consider a system modeled by

$$\ddot{y}(t) + 4\dot{y}(t) + 2y(t) = 3u(t)$$

- Calculate the closed-loop transfer function (with a proportional gain  $k$ ).
- What is the static error for  $k = 1$ ?
- Calculate the value of  $k$  to have a static error = 5%. How much is the overshoot for that value?
- Design a phase lag controller.
- Simulate all these cases with Xcos.

## Exercise 2

We now consider a ball and beam system



A simple model is given by

$$m\ddot{x}(t) = mg \sin(\theta(t)) \quad \Rightarrow \quad \text{linearizing :} \quad \ddot{x}(t) = g\theta(t)$$

- Is the open-loop system stable?
- Is the closed-loop system stable?
- Design a phase lead controller.
- Simulate all these cases with Xcos.